

1. Given a random sample of size  $n$  from a population with mean  $\mu$  and variance  $\sigma^2$ , show that the statistic

$$\frac{1}{n} \sum_{i=1}^n (X_i - \mu)^2$$

is an unbiased estimator of  $\sigma^2$ . How is this statistic different from the sample variance?

2. If  $\Theta_1$  and  $\Theta_2$  are unbiased estimators of the same parameter  $\theta$ , what condition must be imposed on the constants  $k_1$  and  $k_2$  so that the statistic

$$k_1\Theta_1 + k_2\Theta_2$$

is an unbiased estimator of  $\theta$ ?

3. If  $X_1, X_2, \dots, X_n$  constitute a random sample from a population with mean  $\mu$ , what condition must be imposed on the constants  $a_1, a_2, \dots, a_n$  so that the statistic

$$a_1X_1 + a_2X_2 + \dots + a_nX_n$$

is an unbiased estimator of  $\mu$ ?

4. If a random sample of size 20 from a normal population with variance 225 has a mean of 64.3, construct a 95% confidence interval for the population mean  $\mu$ .
5. An industrial engineer wants to determine the average amount of time it takes an adult to assemble an "easy-to-assemble" toy. Use the following random sample data (in minutes) to construct and interpret a 95% confidence interval for the mean of the population.

17	13	18	19	17	21	29	22	16	28	21	15
26	23	24	20	8	17	17	21	32	18	25	22
16	10	20	22	19	14	30	22	12	24	28	11

6. A study is made to determine the proportion of voters in a sizeable community who favor the construction of a nuclear power plant. If 140 of 400 voters selected at random favor the project, construct and interpret a 99% confidence interval for the actual proportion of the population that favors the nuclear plant.